TORSIONAL VIBRATIONS OF CAR CRANKSHAFT ENGINE TAKING INTO ACCOUNT ELEMENTS OF TRANSMISSION

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Abstract. The article is devoted to assessing the influence of the parameters of car transmission elements on the nature of the resulting torsional vibrations of the crankshaft of its power plant. As a rule, at present, the study of torsional vibrations of the crankshafts of piston internal combustion engines is carried out separately from the conditions of their operation. Only the operating modes of the engines, the torques of individual cylinders are considered, taking into account the order of operation and the angle between the flashes. If necessary, instead of a linear equivalent torsional circuit, branched circuits are considered that take into account the influence of individual engine mechanisms. Perturbing moments in such schemes occur only on the crank of the crankshaft. Only engine operating modes are considered, which take into account the elements of the car transmission and their influence on the nature of torsional vibrations along the entire length of the driven shaft. The moments of inertia of each transmission element and the stiffness of the equivalent torsional circuit sections are determined. The oscillation equations of the equivalent design scheme are drawn up taking into account the transmission elements. The values of the natural oscillation frequencies are determined by solution of homogeneous differential equations. The influence of the external environment can be estimated by applying perturbing the moment per equivalent mass replacing elements of the undercarriage of the car. Given the large values of the moments of inertia of the elements of transmission and the frequency range of their own vibrations, it is possible to explain the displacement of the amplitude of vibrations and their nodes. The considered technique is of interest for scientific and technical workers, and designers involved in the design of transmission elements for motor vehicles.

Keywords: transmission, car, scheme, rigidity, shaft, elasticity, deformation, engine, crankshaft, oscillation.

Introduction

During operation of tractor engines, torsional vibrations occur not only in the engine itself, but also in the engine-transmission-drive wheel system. The source of such vibrations is the torques acting on the cranks and the phase-shifted torques of the various cylinders. It is very important to predict such phenomena at the design stage, which reduces further changes in the design and kinematic parameters of the transmission [1; 2]. The correct choice of the dimension of the calculation scheme strongly affects the results obtained. Correct determination of the elastic and inertial parameters of the elements of the design scheme depends on its natural oscillation frequencies and resonant operating modes [3; 4]. The calculation of torsional vibrations of the crankshafts of tractor engines is usually carried out separately for the engine itself. In operational conditions, when the engine is running as part of a mobile transport vehicle, additional masses are added to the oscillatory circuit, which leads to changes in the parameters of the oscillatory process [5; 6]. As a result, it is necessary to change the parameters of the designed torsional vibration dampers [7] to increase the efficiency of their operation. As a rule, such works are accompanied by experimental studies to clarify the influence of transmission elements on the parameters of the oscillatory process [7; 8].

Status of the issue

The typical method of calculating the crankshaft consists of the following steps [9-11]:
1. selection of an equivalent torsion circuit and calculating its parameters;
2. determination of the natural frequencies of torsional vibrations and the corresponding resonant modes of engine operation;
3. harmonic analysis of the engine torque at all resonant operating modes;
4. calculation of the motor mass oscillation amplitudes;
5. determination of emerging additional elastic moments and stresses from them.

This technique is described in [12; 13] and we will not talk about it in detail.

For a comparative analysis, consider the O6 opposed spark engine in the composition of a mid-range car with the following characteristics:

- nominal power/rotation frequency $- N_{eN} = 170$ kW/$n_{eN} = 5800$ rpm;

- cylinder bore/piston stroke – $D = 0.095$ m/S $= 0.073$ m;
- diameter/root collar length – $d_r = 0.055$ m/$l_r = 0.025$ m;
- diameter/connecting rod neck length – $d_{cr} = 0.055$ m/ $l_{cr} = 0.025$ m;
- thickness/cheek width – $e = 0.008$ m/$h = 0.1$ m;
- crank radius – $r = 0.0366$ m;
- layout scheme – oppositional;
- number of cylinders – 6;
- cylinder operation procedure – 1-6-2-4-3-5;
- stroke of the piston – 0.0732 m;
- working volume of the engine – 0.003 m^3.

The design parameters of the transmission elements for the selected car are available in the technical literature [14].

For the calculations of the engine for torsional vibrations, a seven-mass equivalent scheme was chosen, the principles of which are shown in Fig. 1.
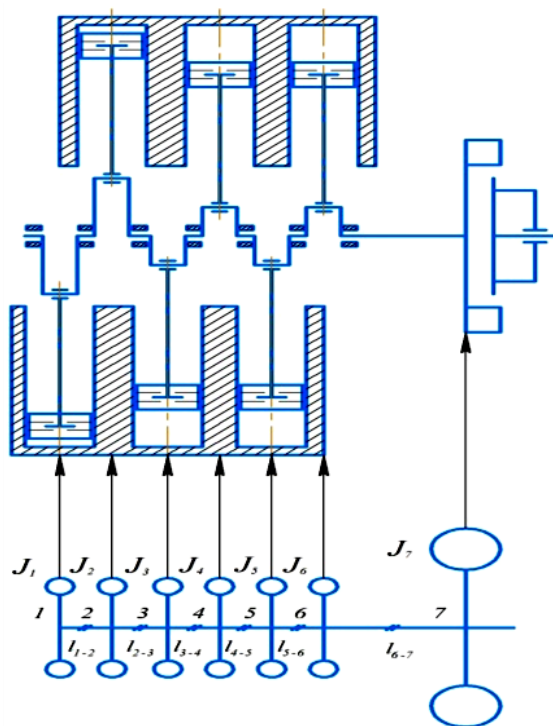

Fig. 1. **Valid and calculated diagram of O6 engine:** J_1, J_2, J_3, J_4, J_5, J_6 – moments of inertia of the motor masses, J_7 – moment of inertia of the flywheel with the clutch, $l_{i\text{-}i+1}$ – length between the i-th and $i+1$-th sections of the equivalent torsional scheme

Using the computational and graphical method, we determine the parameters of the equivalent torsional circuit (Table 1). To simplify the calculations, we accept the assumption about the identity of the plots between the motor masses [15].

Table 1

Parameters of the equivalent torsional sheme

Moment of inertia J_i, kg·m^2	Reduced length $l_{i\text{-}i+1}$, m	Plot stiffness, $C_{i\text{-}i+1}$, N·m
$J_1 = 3.627602\cdot10^{-3}$	-	-
$J_2 = 3.627602\cdot10^{-3}$	$l_{1\text{-}2} = 0.0967$	$C_{1\text{-}2} = 3.53993\cdot10^5$
$J_3 = 3.627602\cdot10^{-3}$	$l_{2\text{-}3} = 0.0967$	$C_{2\text{-}3} = 3.53993\cdot10^5$
$J_4 = 3.627602\cdot10^{-3}$	$l_{3\text{-}4} = 0.0967$	$C_{3\text{-}4} = 3.53993\cdot10^5$
$J_5 = 3.627602\cdot10^{-3}$	$l_{4\text{-}5} = 0.0967$	$C_{4\text{-}5} = 3.53993\cdot10^5$
$J_6 = 3.627602\cdot10^{-3}$	$l_{5\text{-}6} = 0.0967$	$C_{5\text{-}6} = 3.53993\cdot10^5$
$J_7 = 1.041727\cdot10^{-2}$	$l_{6\text{-}7} = 0.0505$	$C_{6\text{-}7} = 6.76655\cdot10^5$

To determine the natural oscillation frequencies, the application software package "MATLAB" is used and the program for working with spreadsheets "Microsoft Excel".

After holding a range analysis (Fig. 2), the value of the natural frequency is selected $\omega_{0} = 2780$ s^{-1}.
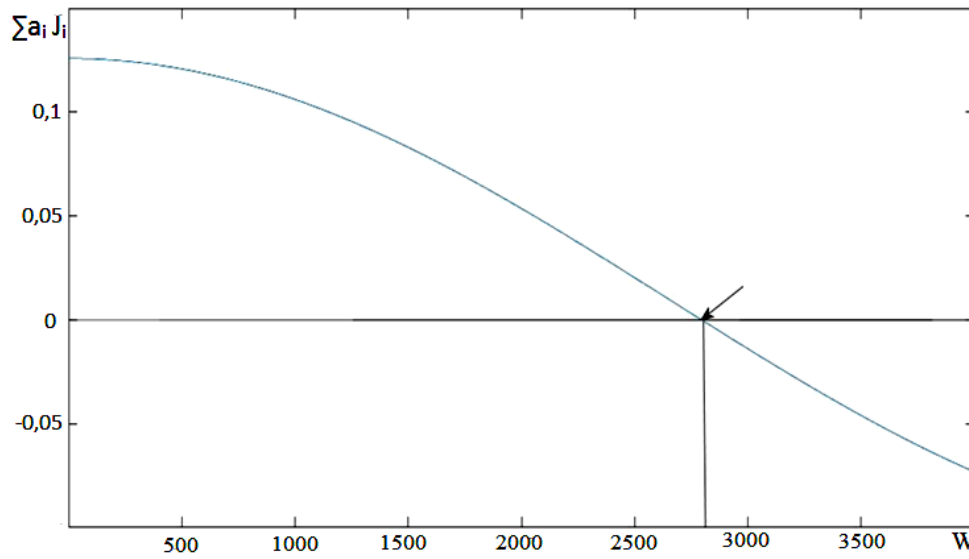

Fig. 2. **Determination of the frequency of natural vibrations by the Holzer method**

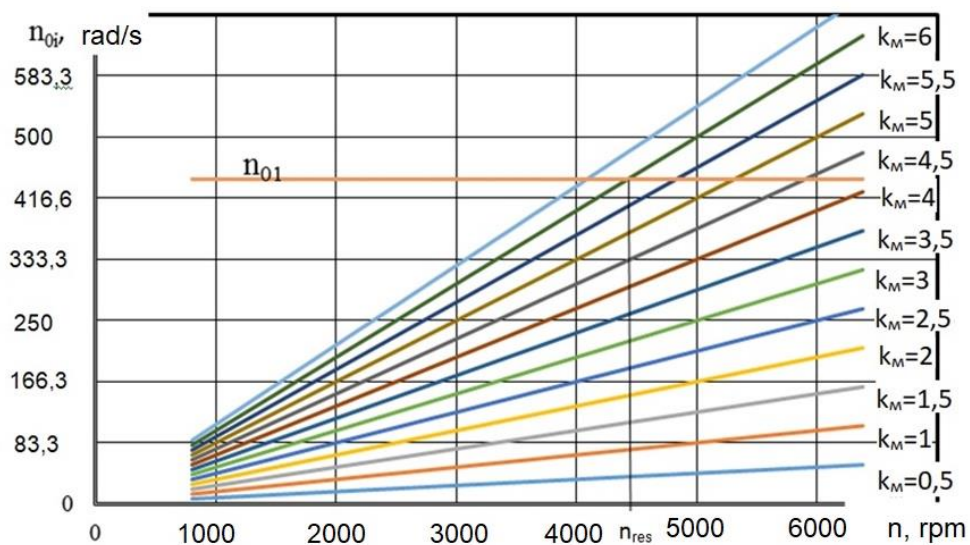To determine the resonant modes of operation, we use the frequency diagram (Fig. 3).

Fig. 3. **Definition of resonant operating modes**

From the resonance condition $n_{0i} = n_k$, the resonant operating mode is established at $n_{res} = 4426$ rpm and $k_{\text{м}} = 6$.

We perform a harmonic analysis of the torque and calculate the motor harmonics.

$$M_t(t) = M_{average} + \sum_{k=0.5}^{15} M_t \cdot \sin(k_m \cdot \varphi + \varphi_{k_m}), \tag{1}$$

where $M_{average} = \frac{1}{N}\sum_{i=0}^{N} y_i$ – average torque acting on the knee;
   $k_m = 0.5k = 0.5; 1; 1.5 ;…; 15$ – motor harmonic index;
   φ_k – k-th harmonic phase shift.

The harmonic analysis results for the O6 engine are shown in Table 2.

Table 2

Harmonic analysis results for O6 engine

k	A_k	B_k	M_k	φ_k
1	-82.863	-57.248	100.715	55.360
2	48.629	125.322	134.427	21.208
3	-10.995	-95.504	96.134	6.567
4	9.373	-165.810	166.074	-3.236
5	10.108	-64.273	65.062	-8.937
6	-9.445	-46.893	47.834	11.388
7	15.508	-41.563	44.362	-20.462
8	-14.784	23.591	27.841	-32.075
9	15.685	-25.313	29.778	-31.784
10	-13.556	19.321	23.602	-35.054
11	12.987	-14.687	19.605	-41.485
12	-11.208	11.564	15.979	-43.640

The next step is to determine the relative amplitudes of motor masses and select the parameters of single-node oscillations (Fig. 4).

Further calculation for additional resonant voltages is subject to a resonance mode with a harmonic $k_M = 6$, because in this mode we have a resonance with the most dangerous main harmonic, as well as a resonant crankshaft speed $n_{res.(6,0)} = 4426$ rpm lies in the operating range of the engine [16; 17].
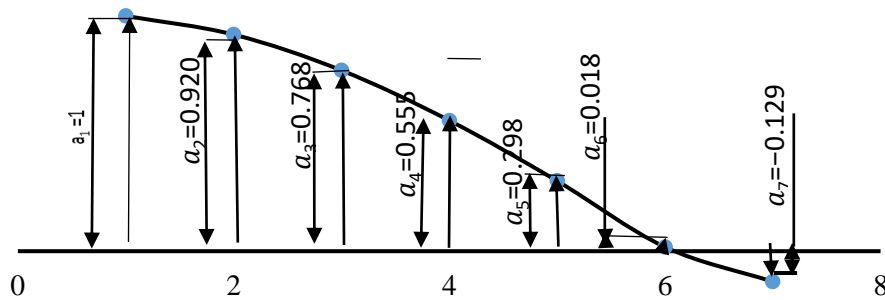

Fig. 4. **Single-node shape of the crankshaft oscillation**

Then using the formula we determine the absolute amplitude of the oscillations of the first motor mass for the absolute value of the torque:

$$A_1^* = \frac{M_t\sqrt{\left[\sum_{i=1}^N a_i^* \sin(k_M \Delta\theta_{1-i})\right]^2 + \left[\sum_{i=1}^N a_i^* \cos(k_M \Delta\theta_{1-i})\right]^2}}{\xi k_M \omega_{ICE} \sum_{i=1}^N (a_i)^2}, \qquad (2)$$

where ξ – damping coefficient;

   ω_{ICE} – angular velocity of the engine crankshaft for the design mode.

The calculation results for even harmonics are shown in Table 3.

Table 3

Calculation results for even harmonics

k_M	1	2	3	4	5	6
M_t, N·m	134.43	166.07	47.83	27.84	23.602	15.979
A_1, rad	0.001998	0.002468	0.003792	0.000414	0.000351	0.001267
A_2, rad	0.001839	0.002272	0.003492	0.000381	0.000323	0.001166
A_3, rad	0.001536	0.001897	0.002915	0.000318	0.000270	0.000974
A_4, rad	0.001110	0.001371	0.002107	0.000230	0.000195	0.000704
A_5, rad	0.000597	0.000737	0.001133	0.000124	0.000105	0.000378
A_6, rad	0.000036	0.000044	0.000068	0.0000074	0.0000063	0.0000228
A_7, rad	-0.0002588	-0.0003198	-0.0004913	-0.0000536	-0.0000454	-0.0001641

The last step in the calculations is to determine additional resonant voltages. To do this, we find the values of the elastic moment for each section of the equivalent shaft according to the formula:

$$M_{el\ i-i+1} = c_{i-i+1}(A_i^* - A_{i+1}^*),$$ (3)

where c_{i-i+1} – stiffness of the equivalent shaft between the i and $i+1$ motor masses.

The calculated values of the elastic moments are given in Table 4.

Table 4

Calculated values of elastic moments

Plot number	1-2	2-3	3-4	4-5	5-6	6-7
$M_{el\ i-i+1}$, N·m	40.623	78.026	109.251	131.824	143.956	144.687

The stresses are calculated on the last section of the shaft, where the greatest elastic moment acts. In our case, this is the last plot.

$$\tau = \frac{M_{el}}{W} = \frac{144,687 \times 16 \times 10^{-6}}{3.14 \times 45^3 \times 10^{-9}} = 8,09\ \text{MPa},$$ (4)

where W – moment of resistance of the shaft cross section.

Consider the calculation of the torsional vibrations of the engine crankshaft together with the transmission of the car (Fig. 5). In this case, the number of masses of the calculated scheme will grow from 7 to 13.
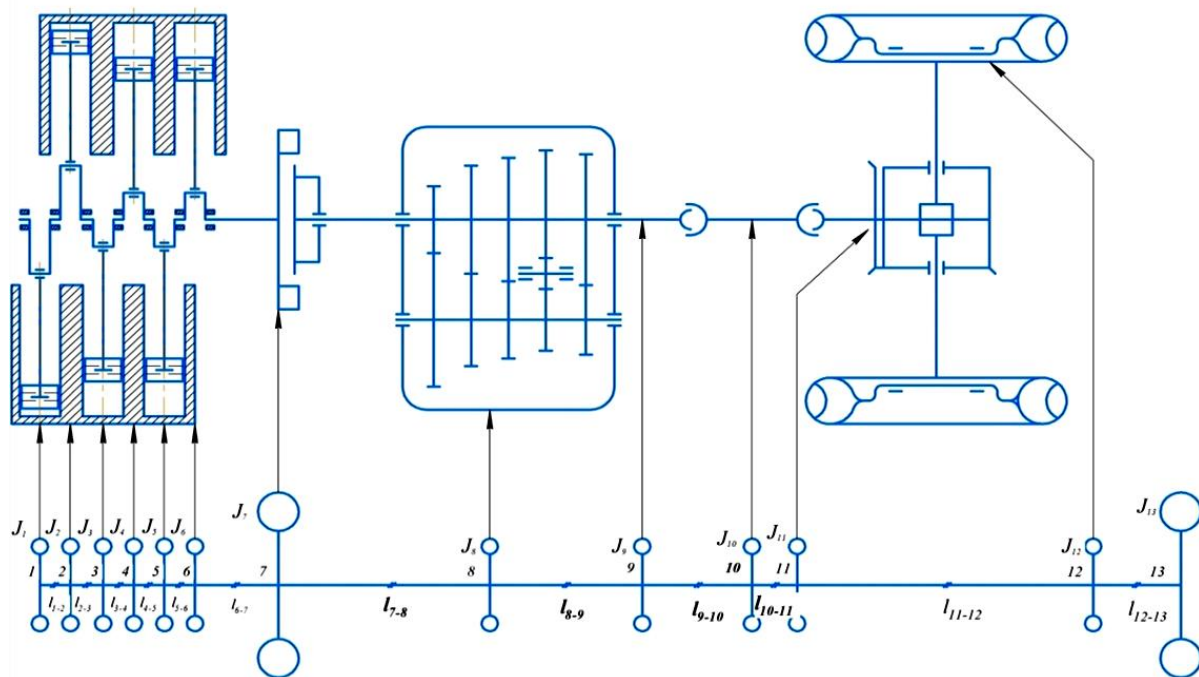

Fig. 5. **Valid and calculated schematics of O6 engine with transmission:**
$J_1, J_2, J_3, J_4, J_5, J_6$ – moments of inertia of motor masses; J_7 –inertia moment of the flywheel with a clutch; J_8 – moment of inertia of the primary and secondary shafts with pinions; J_9 – moment of inertia of the secondary shaft with pinions; J_{10} – moment of inertia of the driveshaft; J_{11} – moment of inertia of differential; J_{12} – moment of inertia of the semi-axes; J_{13} – given moment of inertia of the car at full load; l_{i-i+1} – length between the i-th and $i+1$-th sections of the equivalent torsional scheme.

By analogy with the previously adopted calculation method, we carry out the calculation for torsional vibrations of the crankshaft-transmission system of the car. The design scheme consists of 13 masses. Harmonic torque analysis remains the same.

Additional parameters of the equivalent torsional circuit are shown in Table 5.

Table 5

Additional parameters of the equivalent torsional circuit

Moment of inertia J_i, kg·m²	Reduced length $l_{i\text{-}i+1}$, m	Plot stiffness, $C_{i\text{-}i+1}$, N·m
$J_8 = 19 \cdot 10^{-4}$	$l_{7\text{-}8} = 14.8$	$C_{7\text{-}8} = 0.874 \cdot 10^4$
$J_9 = 2.36 \cdot 10^{-4}$	$l_{8\text{-}9} = 385.95$	$C_{8\text{-}9} = 0.0335 \cdot 10^4$
$J_{10} = 3.01 \cdot 10^{-4}$	$l_{9\text{-}10} = 53.23$	$C_{9\text{-}10} = 0.243 \cdot 10^4$
$J_{11} = 1.56 \cdot 10^{-4}$	$l_{10\text{-}11} = 759.19$	$C_{10\text{-}11} = 0.017 \cdot 10^4$
$J_{12} = 0.0105$	$l_{11\text{-}12} = 778.82$	$C_{11\text{-}12} = 0.0166 \cdot 10^4$
$J_{13} = 0.724$	$l_{12\text{-}13} = 231.12$	$C_{12\text{-}13} = 0.056 \cdot 10^4$

Set a new resonant mode of operation is set at $n_{res} = 17.4$ s^{-1} and $k_M = 6$.

The calculated values of the absolute amplitudes of oscillations of motor masses for even harmonics are given in Table 6.

Table 6

Calculated values of the absolute amplitudes of oscillations of motor masses for even harmonics

k_M	1	2	3	4	5	6
M_k, N·m	134.43	166.07	47.83	27.84	2.602	15,979
A_1, rad	0.001246	0.002002	0.003145	0.000367	0.000291	0.001011
A_2, rad	0.001143	0.001945	0.003012	0.000326	0.000285	0.000967
A_3, rad	0.001012	0.001897	0.002915	0.000318	0.000270	0.000974
A_4, rad	0.000934	0.001371	0.002107	0.000230	0.000195	0.000704
A_5, rad	0.000578	0.000737	0.001133	0.000124	0.000105	0.000378
A_6, rad	0.000027	0.000044	0.000068	0.0000074	0.0000063	0.000228
A_7, rad	0.000157	0.0003198	0.0004913	0.0000536	0.0000454	0.000164
A_8, rad	-0.000342	-0.000573	-0.000736	-0.000156	-0.0001587	-0.000127
A_9, rad	-0.00256	-0.00387	-0.00987	-0.000693	-0.000578	-0.000873
A_{10}, rad	-0.00637	-0.00734	-0.01258	-0.001025	-0.000973	-0.00157
A_{11}, rad	-0.00845	-0.00912	-0.01387	-0.001578	-0.001323	-0.00478
A_{12}, rad	-0.00893	-0.00987	-0.01578	-0.001934	-0.002198	-0.00856
A_{13}, rad	-0.00967	-0.01023	-0.01734	-0.002498	-0.004213	-0.00978

Consider only the plot of the crankshaft (Table 7) and determine for it the elastic moments and emerging additional stress from torsional vibrations.

Table 7

Elastic moments and the resulting additional stresses from torsional vibrations

Plot number	1-2	2-3	3-4	4-5	5-6	6-7
$M_{el\ i-i+1}$, N·m	35.545	68.274	95.597	115.349	125.964	126.604

$$\tau = \frac{M_{el}}{W} = \frac{126{,}604 \times 16 \times 10^{-6}}{3.14 \times 45^3 \times 10^{-9}} = 7.079 \text{ MPa}.$$

For the calculated section, the additional stresses were reduced by 12% compared to the calculation of the crankshaft without taking into account the elements of the car transmission. In this case, the oscillation node is shifted in the direction of the car transmission, the resonant modes have lower values.

Conclusions

The calculation of the torsional vibrations of the crankshafts of car engines can be entered both separately for the engine and taking into account the other elements of the transmission of the torque to the driving wheels. However, the results of the calculations will differ. The use of a multi-mass design scheme of the crankshaft, taking into account the elements of the car transmission, significantly changes the picture of torsional vibrations: the node of single-node vibrations is shifted towards the car transmission, the resonant modes of operation are shifted towards low frequencies. The amplitudes of the motor mass oscillations also change. In our calculations, the oscillation amplitude of the first motor

mass changed from $A_1 = 0.001998$ rad to $A_1 = 0,001246$ rad, the first resonant frequency changed from $n_{rez} = 4426$ rpm to $n_{rez} = 4045$ rpm. The resulting elastic moment on the most dangerous section 6-7 of the shaft changed from $M_{el.6-7} = 144.687$ Nm to $M_{el.6-7} = 124.604$ Nm. This must be taken into account, when designing and determining the effective modes of operation of torsional vibration dampers of crankshafts.

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